Effect of swirl flow on the performance of parallel hub axial annular diffuser

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ABSTRACT

In the present work, the parallel hub axial flow annular diffuser's performance characteristics with divergent casing varying between equivalent cone angle (10°, 15°, and 20°) with area ratio 3 have been evaluated computationally as well as experimentally. The performance of three diffusers were tested at different inlet swirl angles (from 0° to 25°) for swirling and non-swirling flow. Simulations have been carried out on a fully developed flow at Reynolds number 2.5×10^5. The results were analyzed based on the velocity profiles, static pressure recovery coefficient, and the total pressure loss coefficient. The result analysis shows that the inlet swirl flow improves the recovery of pressure and also delays the flow separation on the casing. Moreover, the findings also show that the best performance was achieved in equivalent cone angle 10° at the inlet swirl angle of 7.5° compared to other diffusers.

Key words: Annular diffuser; Static pressure recovery coefficient; Total pressure loss coefficient; Inlet swirl angle.

INTRODUCTION

The annular diffuser is a mechanical flow diffusing device that is used for many engineering applications. The diffuser's primary function is to recuperate the static pressure due to reducing the flow's mean velocity. The Annular diffuser is mainly used in the pump, compressor, gas turbine engine, turbomachinery, etc. (Kline, 1959). The fluid flow around the bearing, vanes,
and strut creates a swirl effect at the diffuser's entry. The swirl effect at the inlet is one way to increase the overall performance of the diffuser. Reneau et al. (1967) experimentally examined the effect of flow characteristics on two-dimensional straight wall diffusers. It was found that diffuser performance decreases as the inlet blockage increases in the two-dimensional conical diffusers. Coladipietro (1974) studied the inlet swirl and boundary layer thickness effect on the performance of diffusers. The efficiency and pressure recovery coefficient were more pronounced in a thin boundary layer for a small non-dimensional length. Adenubi (1976) experimentally studied the flow regimes of straight core annular diffuser with downstream turbo machine inlet conditions. It was observed that the annular diffuser's effectiveness enhances by increasing the turbulence level at the inlet. Singh et al. (1994) found that swirl improved the recovery of pressure and suppressed the separation of flow on the casing in the wide-angle annular diffuser. Mohan et al. [1998] analyzed the optimum performance of the diffusers with the computational approach with less cost than the experimentation. It shows that maximum pressure recovery improvement is achieved at a 17.5° diffuser. Shuja and Habib (1996) studied the axisymmetric annular diffuser and concluded that the increase in the flow region's heat transfer coefficient depends on the cant angle. They have also shown that the Nusselt number is a function of the Reynolds number. Ubertini and Desideri (2000) described the gas turbine annular exhaust diffuser with and without strut as having effectiveness 15 percent and less than 15 percent, respectively. It is shown that overall diffuser losses enhanced in the axial region of a strut. Arora and Pathak (2009); Arora et al. (2010); Arora (2014); Singh and Arora (2019) carried out the experimental and numerical investigation of geometrical parameters on the annular diffuser with swirl flow. They concluded that the recovery of static pressure is faster with the introduction of swirl at the diffuser's entry.

Very little research work has been carried out experimentally on the swirl flow in annular diffusers. Based on the exhaustive literature review, it is very difficult to conclude
which choice of geometric parameters and dynamic parameters will give diffusers the desirable performance because the fluid flow is quite complicated. Since there is no research work carried out on the different cone angles and has the same area ratio, it needs to be explored. The main work is focused on the parallel hub axial annular diffuser with varying geometries but having the same area ratio 3. The effect of swirl intensity is analyzed with different swirl regimes on the flow characteristics of annular diffusers. Further, the prediction of the flow separation and reattachment of the flow are carried out inside the annular diffusers. Figure 1 and Table 1 show the geometrical configuration details of the parallel hub axial annular diffuser parameters.

**Table 1** Geometrical parameters of parallel hub axial annular diffusers.

<table>
<thead>
<tr>
<th>Sr. No.</th>
<th>$\theta_c$ (deg)</th>
<th>L(cm)</th>
<th>$L/\Delta R$</th>
<th>$\theta_e$ (deg)</th>
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<tr>
<td>A</td>
<td>4.6</td>
<td>56.51</td>
<td>14.30</td>
<td>10</td>
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<tr>
<td>B</td>
<td>6.91</td>
<td>37.55</td>
<td>9.50</td>
<td>15</td>
</tr>
<tr>
<td>C</td>
<td>9.22</td>
<td>28.04</td>
<td>7.09</td>
<td>20</td>
</tr>
</tbody>
</table>

**Figure 1** Diffuser geometrical parameter.

**EXPERIMENTAL SET UP**

Figure 2 (i) shows the annular diffuser experimental set up used for experimentation. Figure 2 (ii) represents the setup's main components i.e. blower, settling chamber, swirl plate, annular passage, and diffuser. The centrifugal blower sucks air from the ambiance then delivers it to the settling chamber with a conical divergence section, which is precisely aligned with the settling chamber. The airflow rate is controlled by changing the rpm of the impeller and throttling valve placed at the inlet. The settling chamber consists of a honeycomb and different mesh screen
sizes to prevent the flow fluctuation, reduce turbulence, and make the flow uniform. A well designed conical contraction zone of settling chamber connected to the long annulus passage in which flow commences. The swirl plate is located upstream of the test diffuser to avoid the wake effect at the test diffuser's entry to recover the pressure. Test diffuser made of transparent Perspex and hub casted of aluminum material, which is perfectly machined to get a smooth surface fabricated with a precision of ±1 percent tolerance. The numbers of static pressure taps on the casing and hub wall are made along the test diffuser's length to measure static pressure with manometers. The manometers are inclined at an angle of 10° with the horizontal to increase the sensitivity of reading. The longitudinal velocity and swirl velocity are measured along with the test diffuser's axial locations using a three-hole cobra probe using the null technique (Bryer and Pankhurst, 1971). The cobra probe yaw angle is set to zero by aligning with the incoming flow in this technique. The calibration range is associated with the cobra probe to measure the velocity within ±55 deg. The manometer's uncertainty for measurement of the static pressure is ± 1.5 mm of water, and the total pressure is ±1 mm of water.

![Figure 2](image)

**Figure 2** (i) Experimental set up; (ii) Schematic of the experimental set up.

**MATHEMATICAL FORMULATIONS**

The equation of continuity in 2D axisymmetric geometry is given as

\[
\frac{\partial}{\partial x} (\rho v_r) + \frac{\partial}{\partial r} (\rho v_r) + \frac{\rho v_r}{r} = s_m
\]

(1)
Where \( v_x \) is the axial direction velocity, and \( v_r \) is the radial direction velocity. \( \dot{m} \) is the mass added to the continuous phase from the dispersed phase.

The governing equations of momentum conservation for steady axisymmetric non-swirling flow in the axial and radial directions are given as

\[
\frac{1}{r} \frac{\partial}{\partial x} (r \rho v_x v_x) + \frac{1}{r} \frac{\partial}{\partial r} (r \rho v_r v_r) =
- \frac{\partial p}{\partial x} + \frac{1}{r} \frac{\partial}{\partial x} \left[ r \mu \left( 2 \frac{\partial v_x}{\partial x} - \frac{2}{3} (\nabla \cdot v) \right) \right] + \frac{1}{r} \frac{\partial}{\partial r} \left[ r \mu \left( \frac{\partial v_x}{\partial r} + \frac{\partial v_r}{\partial x} \right) \right] + F_x \tag{2}
\]

And

\[
\frac{1}{r} \frac{\partial}{\partial x} (r \rho v_x v_r) + \frac{1}{r} \frac{\partial}{\partial r} (r \rho v_r v_r) =
- \frac{\partial p}{\partial r} + \frac{1}{r} \frac{\partial}{\partial x} \left[ r \mu \left( \frac{\partial v_r}{\partial x} + \frac{\partial v_x}{\partial r} \right) \right] + \frac{1}{r} \frac{\partial}{\partial r} \left[ r \mu \left( \frac{2}{3} \frac{\partial v_r}{\partial r} - \frac{2}{3} (\nabla \cdot v) \right) \right]
- 2 \mu \frac{v_r}{r} + \frac{2}{3} \frac{\mu}{r} (\nabla \cdot v) + \rho \frac{v_r^2}{r} + F_r \tag{3}
\]

Where

\[
\nabla \cdot v = \frac{\partial v_x}{\partial x} + \frac{\partial v_r}{\partial r} + \frac{v}{r} \tag{4}
\]

Here \( F_x \) and \( F_r \) represent axial and radial forces respectively.

The tangential momentum equation for swirling flows need to be solved, which can be written as

\[
\frac{1}{r} \frac{\partial}{\partial x} (r \rho v_x v_z) + \frac{1}{r} \frac{\partial}{\partial r} (r \rho v_r v_z) =
1 \frac{\partial}{\partial x} \left[ \frac{r \mu}{r} \frac{\partial v_z}{\partial x} \right] + 1 \frac{\partial}{\partial r} \left[ r^3 \mu \frac{\partial}{\partial r} \left( \frac{v_z}{r} \right) \right] - \rho \frac{v_z v_z}{r} \tag{5}
\]

Where \( v_z \) represents the swirl velocity.
The turbulent flow parameters are computed, turbulence models are analyzed to the close solution of the RANS set of equations (1-5). The selection of turbulence models such as $k-\varepsilon$ standard, $k-\omega$ standard, $k-\varepsilon$ Realizable, $k-\varepsilon$ RNG, and $k-\omega$ SST on the annular diffuser with swirl flow is a complicated process. The RNG $k-\varepsilon$ turbulence model is a more advanced model as compared to the $k-\varepsilon$ standard model.

Mohan et al. (1998); Singh et al. (2006); Arora and Pathak (2009); Arora et al. (2010) have adopted two-equation turbulence model $k-\varepsilon$ RNG on annular diffusers for their work while work using $k-\varepsilon$ Standard model was carried out by Sadasivan et al. (2019). The result from the simulation of a non-dimensional longitudinal velocity profile distribution at $x/L=0.7$ is shown in Figure 3. It is seen that the $k-\varepsilon$ RNG turbulence model gives the lowest average deviation as compared to the experimental results. Hence $k-\varepsilon$ RNG turbulence model is employed for simulation in the present study.

**Figure 3** Comparison of the turbulence models with the experimental results of the longitudinal velocity profile at $x/L=0.7$ of equivalent cone angle 10°.

**COMPUTATIONAL DOMAIN AND BOUNDARY CONDITIONS**

An axis-symmetric two-dimensional computational domain of the annular diffuser has been sketched in the ANSYS Fluent v16.2 software. A map meshing scheme has been used with a quadrilateral element to carry out the simulations. The 2D mesh geometry of the computational domain has been shown in Figure 4. Very fine mesh is placed near the wall by maintaining the
y+<1. The first node of the mesh is placed at a distance of 0.02mm from the wall to predict the velocity gradient near the wall. The quality of the mesh is maintained in terms of skewness, aspect ratio, and orthogonality. The inlet velocity profile is fed in the axisymmetric diffuser similar to the velocity profile obtained from the experimental setup. The turbulent intensity 3% is applied at the inlet, and the value of the hydraulic diameter is calculated as per the diffuser's geometry. The boundary conditions at the outlet are applied 3% turbulent intensity normal to the boundary, zero gauge pressure, and thus calculated value of the hydraulic diameter (h_d) from the geometry of diffuser. The 2\textsuperscript{nd} order upwind scheme is used to control the solution for swirl velocity, momentum, turbulent kinetic energy (k), and turbulent dissipation rate (\omega) for better accuracy of results. The employed residuals for convergence criteria is $10^{-6}$ to achieve convergence solution by an iteration method. The SIMPLE algorithm method is used for the stability of the solution.

![Figure 4 2D axisymmetric computational domain with meshing.](image)

**GRID INDEPENDENCE TEST**

In the current work, a grid test is carried out to obtain mesh independence results. The different diffusers having various geometrical designs will have different grid sizes depending upon the geometrical dimension.
In the parallel hub axial annular diffuser having an equivalent cone angle 10° with area ratio 3 of four grid sizes (mesh 1=90000, mesh 2=120000, mesh 3=160000, and mesh 4=190000) were tested at Reynolds number $2.5 \times 10^5$ using k-ε RNG turbulence model for swirl flow. Pressure coefficient profiles for Mesh 3 and Mesh 4 are very close to each other, and hence cell count of Mesh 3 is selected for the current study, as shown in Figure 5. The simulation is performed on the i5 processor with 8GB RAM, and the time required to solve the simulation of 160000 elements is 18hrs.

**RESULTS AND DISCUSSION**

The computationally determined velocity vectors, longitudinal velocity profiles, swirl velocity profiles, static pressure recovery coefficient ($C_p$), and total pressure loss coefficient ($C_{TL}$) across the diffuser's length are presented and discussed.

**Velocity vector**

The axisymmetric 2D annular diffusers (A, B, and C) with and without swirl flow of velocity vectors at the inlet swirl angles (0°, 12°, and 25°) are shown in Fig. 6. The velocity vectors show the result across the length i.e. inlet, $x/L=0.1,0.3,0.5,0.7,0.9$, and outlet using CFD.
The uniform flow is distributed between the casing and hub wall at swirl angles 0°, and 12° as flow moves toward the downward direction in the diffuser A. The flow separation is observed on the inner wall at the inlet swirl angle 25° along the two-thirds length of diffuser A. In diffuser B, the reverse flow is observed at the swirl angles 12° and 25° on the hub walls due to the adverse pressure gradient. The high casing divergent angle in diffuser C due to that flow separation is observed on the casing wall with the non-swirling flow. The separation zone's size increases with the inlet swirl angles (12° and 25°) and results in the shifting of flow separation position and negative velocity towards the hub wall. For the 25° inlet swirl angle, the flow visualization in the velocity vectors shows that flow is accumulated on the casing wall, and a large separations zone exists on the hub wall.

**Figure 6** (i-x) Velocity vectors at inlet swirl angles 0°, 12°, and 25° of equivalent cone angle 10°, 15°, and 20°.

*Velocity profile*
The flow behavior and performance of diffuser (A) have been shown in Figures (7-8) in the form of longitudinal velocity profiles and swirl velocity profiles concerning average mass velocity with different inlet swirl conditions i.e. 0°, 12°, and 25°. The hub position represents as y/Ym =0, and the casing position represents as y/Ym = 1 (Klomp, 1997). The graphs shown in Figures (7-8) are drawn at different location i.e. x/L = 0.1, 0.3, 0.5, 0.7, and 0.9 for diffuser A of area ratio 3. For no swirl condition, flow is accumulated near the hub wall at an equivalent cone angle of 10°, as shown in Figure 7 (i). The velocities recede at a faster rate on the walls as the continuous diffusion occurs throughout the diffusers. The tangential movement generated by the swirl 12° is not enough to move the bulk flow from the hub wall to the casing wall, as shown in Figure 7 (ii). Figure 7 (iii) shows a reversal trend for a 25° swirl in the longitudinal velocity distribution. In this case, bulk flow moves toward the casing wall. The reversal of flow at swirl angle 25° for x/L=0.5,0.7 and 0.9 is reversed up to the y/Ym=0.18,0.25, and 0.27, respectively. Figure 8 (i-ii) shows swirl velocity distribution at the 12°and 25° inlet swirl angles. The trends are similar for 12°and 25° swirl angles, but the value of magnitude is different. The bulk flow forced towards the casing in the case of a swirl angle 25°. These trends are based on the conservation of the angular momentum principle. The flow is moving towards the casing wall by introducing a swirl at the inlet.
Figure 7 (i-iii) Longitudinal Velocity distribution at inlet swirl angles 0°, 12°, and 25° of equivalent cone angle 10°.

Figure 8 (i-ii) Swirl Velocity distribution at inlet swirl angles 12° and 25° of equivalent cone angle 10°.

Pressure recovery coefficient

The coefficient of pressure recovery has been determined in the annular diffuser having equivalent cone angle 10° with inlet swirl angles 0° to 25° at the diffuser's casing wall. The graph is shown in Figure 9 (i) for area ratio 3 with normalized axial length x/L (Ibrahim et al. 2007). It can be seen from plots that Cp increases with the flow downstream of the diffuser passage. The curves drawn represent the value of Cp for swirl flow almost identical to the 0° swirl. The figure shows that marginal Cp improves with the downstream diffuser passage in
the beginning and later on decreases due to separation of flow on the hub as observed from the longitudinal velocity profile distribution. Swirl increases the \( C_p \) at the entrance of the downstream diffuser passage as compared to the non-swirl flow. The highest \( C_p \) is up to \( x/L=0.18 \) at equivalent cone angle 10° for 25° inlet swirl angles of the diffuser passage. The \( C_p \) plot is shown in Figure 9 (i) shows the maximum improvement of the pressure recovery in an equivalent cone angle of 10° with a 7.5° inlet swirl angle. The variation of static pressure recovery coefficient (\( C_p \)) with the inlet swirl angle of three types of diffusers (A, B, and C) is shown in Figure 10 (i). These plots indicate that there is a maximum coefficient of static pressure recovery with an inlet swirl angles 7.5° and 12° of equivalent cone angles 10° and 15°, respectively. The pressure recovery increases up to \( x/L=0.60 \) and 0.54 for swirl angles 7.5° and 12° respectively of equivalent cone 20° but later on decreases due to separation of flow and decay swirl intensity. The coefficient of static pressure recovery (\( C_p \)) with a variation of the area ratio of diffusers A, B, and C along the length is shown in Figure 10 (ii). It is observed from the figure that maximum pressure recovery is obtained from the equivalent cone angle 10° for an A-type diffuser.

**Figure 9** (i) Pressure coefficient at casing of equivalent cone angle 10°; (ii) Total pressure loss coefficient of equivalent cone angle 10°.

**Total pressure loss coefficient**

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The total pressure loss coefficient increases almost linearly across the longitudinal length. As shown in Figure 9 (ii), the $C_{TL}$ plot shows the minimum loss coefficient for equivalent cone angle $10^\circ$ at $7.5^\circ$ inlet swirl angle. This result implies that the inlet swirl angle's optimum selection suppresses the flow separation. The total pressure loss coefficient ($C_{TL}$) with the swirl angle is shown in Figure 11 (ii). The minimum loss of total pressure coefficient for equivalent cone angle $15^\circ$ is up to $12^\circ$ swirl angle and gives optimum performance at that angle. It also shows the minimum loss of total pressure coefficient at $7.5^\circ$ swirl angle for equivalent cone angle $20^\circ$. The maximum loss coefficient is due to the casing's high cant angle, the swirl intensity's decay, and the adverse pressure gradient on the walls.

Figure 10 (i) Static pressure recovery coefficient with inlet swirl of diffusers A, B, and C; (ii) Static pressure recovery coefficient ($C_p$) with variation of area ratio of diffusers A, B, and C along the length.

**Effectiveness**

The diffuser's effectiveness ($\eta$) is plotted about the inlet swirl angle of A, B, and C types diffusers are shown in Figure 20 (i) (Hoadley, 1970). The plots indicate that $\eta$ decreases with increasing equivalent cone angle and the highest value obtained for the A-type diffuser with a swirl angle of $7.5^\circ$. The diffuser's effectiveness decreases beyond the swirl angle of $12^\circ$ for A and B types diffusers due to the hub's separation and reversal flow. In C type diffuser, the $\eta$ decreases by the swirling flow due to wide space availability, which promotes separation of
flow either from the hub or casing wall, as seen in the velocity vector contours of equivalent cone angle 20°.

Figure 11 (i) Effectiveness with inlet swirl of diffusers A, B, and C; (ii) Total pressure loss coefficient with inlet swirl of diffusers A, B, and C.

CONCLUSION

The following inferences have been highlighted from the numerical investigation of the incompressible flow through the parallel hub axial annular diffuser having equivalent cone angles (10°, 15°, and 20°) and the same area ratio (AR=3).

1. The longitudinal velocity profile is not symmetrical about the center at any cross-section of diffusers. The diffuser’s non-swirling flow is accumulated at the hub, which is shifted towards the casing side with swirl flow.

2. The maximum value of Cp achieved at the exit of the diffuser are 0.75, 0.67 and 0.56, corresponding to 7.5°, 12°, and 0° swirl angle and 10°, 15°, and 20° equivalent cone angles, respectively. Hence it is found that the maximum coefficient of pressure recovery increases up to 75% at swirl angle 7.5° of equivalent cone angle 10° for area ratio 3.

3. The total pressure loss coefficient (C_{TL}) is minimum at the optimum swirl angle along the diffuser passage. The simulated results show that the optimum swirl angles are 7.5° and 12° at equivalent cone angles 10° and 15°, respectively.
4. The stall is observed on the casing for equivalent cone angle 20° in non-swirl flow, but it vanishes and moves away from the casing wall with swirl flow.

**NOMENCLATURE**

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<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Subscripts</th>
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<tr>
<td>θ</td>
<td>Divergence angle of wall, deg;</td>
<td></td>
</tr>
<tr>
<td>ΔR</td>
<td>Annulus height, cm;</td>
<td>c  Casing;</td>
</tr>
<tr>
<td>L</td>
<td>Length of diffuser, cm;</td>
<td>h  hub;</td>
</tr>
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<td>x/L</td>
<td>Non-dimensional axial length;</td>
<td>i  Inlet;</td>
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<td>y/Ym</td>
<td>Non-dimensional radial length.</td>
<td>o  Outlet;</td>
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<tr>
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<td>e  Equivalent.</td>
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**REFERENCES**


